

Program	Level		Third cycle	
	Name of the program		SEE Doctoral Studies in Mathematical Science	
COURSE				
Course title	Spectral theory of automorphic forms			
Course code	Semester	Course status	ECTS	Contact hours
PMAT 665	II	Elective course	10	30
Lecturer	Prof. Dr. Lejla Smajlović			
Course Goals	The main goal of the course is to introduce basic aspects of spectral theory of automorphic forms on Fuchsian groups. To be precise, the goal is to describe spectral expansion of the space of cusp forms and the space of incomplete Eisenstein series and then to derive the Selberg trace formula on noncompact Riemannian surfaces of finite volume. Then, using the trace formula we will introduce the Selberg zeta function and describe its basic properties. As an application of the methods introduced, we will derive the Weyl law for the distribution of eigenvalues of the Laplacian on non-compact Riemannian surfaces of finite volume.			
COURSE CONTENT				
<ul style="list-style-type: none"> - Harmonic analysis on hyperbolic plane: hyperbolic coordinates, classification of isometries, eigenfunctions of the Laplace operator, invariant integral operators, Selberg/Harish-Chandra transform. - Fuchsian groups: definition of a Fuchsian group and its fundamental domain, classification of elements of Fuchsian groups, classification of Fuchsian groups, some special arithmetic Fuchsian groups. - Automorphic forms: definition, definition of a cusp form and Eisenstein series, Kloosterman sums and Fourier expansion of Eisenstein series. - Green's function on the upper half-plane and spectral expansion of the space of cusp forms (as Δ-invariant subspaces). - Automorphic Green function and analytic continuation of Eisenstein series. - Functional equation, poles and residues of Eisenstein series. - Spectral expansion of the space of incomplete Eisenstein series (as Δ-invariant subspaces). - The Selberg trace formula. - The Selberg zeta function, its basic properties and functional equation. - The Weyl law 				
LITERATURE				
[1] H. Iwaniec, Spectral Methods of Automorphic Forms, Graduate Studies in Mathematics, Vol. 53, American Mathematical Society, 2002. [2] H. Iwaniec, E. Kowalski, Analytic Number Theory, AMS Colloquium Publications, Vol. 53, American Mathematical Society, 2004. [3] D. A. Hejhal, The Selberg Trace formula for $PSL(2, \mathbb{R})$, Vol. I, Lecture Notes in Mathematics 548, Springer Verlag, 1976. [4] D. A. Hejhal, The Selberg Trace formula for $PSL(2, \mathbb{R})$, Vol. II, Lecture Notes in Mathematics 1001, Springer Verlag, 1983. [5] J. Fischer, An Approach to the Selberg Trace Formula via the Selberg Zeta Function, Lecture Notes in Mathematics 1253, Springer Verlag, 1987				
GRADING			REMARKS	
Criterion	Maximum points	Minimum points		
Homework	20	11		
Project	40	22		
Final exam	40	22		
T o t a l	100	55		