

Program	Level		First cycle				
	Name of the program		All study programs				
COURSE							
Course title	Dynamical Systems						
Course code	Semester	Course status		ECTS	Contact hours (L+AE+LE)		
AMAT 340	V	Elective course		4	2+2+0		
Lecturer							
Course Goals	The goal of this course is to introduce fundamental techniques for analyzing discrete dynamical systems in one dimension.						
Learning Outcomes	<p>On completion of the course, the student should be able to:</p> <ul style="list-style-type: none"> • explain the basic concept of difference equations; • explain the meaning of the solutions of difference equations; • find equilibrium and periodic solutions to autonomous difference equations, and investigate their stability properties; • analyze difference equations models by using computational and analytic tools; • find and classify by type the bifurcation points of difference equations; • use computer simulations; • apply difference equations in some real-world problems. 						
COURSE CONTENT							
Dynamics of autonomous first-order difference equations. Linear first-order difference equations. Equilibrium points. Graphical iteration and stability. Criteria for stability. Hyperbolic and nonhyperbolic equilibrium points. Period points and cycles. The logistic equation and period-doubling. Bifurcations (Tangent, Transcritical, Period-doubling). Basin of attraction of equilibrium points. Basin of attraction of periodic orbits. Global stability. Applications.							
LITERATURE							
<p>[1] Saber N. Elaydi: Discrete Chaos, 2nd edition, Chapman & Hall/CRC 2007.</p> <p>[2] Saber N. Elaydi: An Introduction to Difference Equations, 3rd edition, Springer 2004</p> <p>[3] Morris W. Hirsch, Stephen Smale, Robert L. Devaney: Differential Equations, Dynamical Systems & An Introduction to Chaos, Elsevier Academic Press 2003.</p> <p>[4] Mustafa R.S. Kulenović, Orlando Merino: Discrete Dynamical Systems and Difference Equations with Mathematica, Chapman & Hall/CRC 2002.</p> <p>[5] Ronald E. Mickens: Difference Equations Theory and Applications, Chapman & Hall/CRC, Second Edition 1998 .</p> <p>[6] C. Robinson: Dynamical Systems, Stability, Symbolic Dynamics and Chaos, CRC Press, 1999.</p>							
STUDENT WORKLOAD (hours in a semester)							
Lectures	30	Tutorial	30	Individual work	40	T o t a l	100
GRADING				REMARKS			
Criterion	Maximum points	Minimum points	<p>Midterm exam: only once in semester (end of November or first week of December). Students altogether write 120 minutes long test. This test is evaluated by max 50 points. The minimal score of the test is 25 points.</p> <p>Final exam: Students who do not reach the midterm exam minimal score must take the entire course in the final exam. In this case, the final exam is evaluated by max 100 points. The final exam's minimal score is 55 points. Students who reach the midterm exam minimal score take only the part of the final exam that is not covered by the midterm test. In this case, the final exam is evaluated by max 50 points. The minimal score is 30 points.</p>				
Midterm exams	50	25					
Homework assignment							
Project							
Laboratory assignments							
Final exam	50	30					
T o t a l	100	55					